

## 14.8 Videos Guide

### 14.8a

- The method of Lagrange multipliers
  - In  $\mathbb{R}^2$  and  $\mathbb{R}^3$ , when optimizing a function  $f$  subject to the equation  $g = c$ , we use the fact that  $\nabla f = \lambda \nabla g$  ( $\lambda$  is called the Lagrange multiplier)

Exercises:

- Find the maximum area for a rectangle inscribed in the ellipse  $\frac{x^2}{3^2} + \frac{y^2}{4^2}$

### 14.8b

- Use Lagrange multipliers to find the extreme values of the function subject to the given constraint.
  - $f(x, y) = 3x + y; \quad x^2 + y^2 = 10$
  - $f(x, y) = xe^y; \quad x^2 + y^2 = 2$

### 14.8c

- $f(x, y, z) = \ln(x^2 + 1) + \ln(y^2 + 1) + \ln(z^2 + 1); \quad x^2 + y^2 + z^2 = 12$

### 14.8d

- Use Lagrange multipliers to find the points on the cone  $z^2 = x^2 + y^2$  that are closest to the point  $(4, 2, 0)$ .

### 14.8e

- When optimizing a function  $f(x, y, z)$  subject to two constraints  $g = k$  and  $h = c$ , we use  $\nabla f = \lambda \nabla g + \mu \nabla h$

Exercise:

- Find the extreme values of  $f$  subject to both constraints.  
 $f(x, y, z) = z; \quad x^2 + y^2 = z^2, \quad x + y + z = 24$